

Introduction to geodynamic modelling

Key physical processes and concepts

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 Present the main physical processes and concepts we need to consider to understand geodynamics (mainly in the lithosphere)

• Provide **necessary background** for the rest of the course



- This course is titled "Introduction to geodynamic modelling"
 - What does this title bring to mind for you?



Dissecting the course title

- This course is titled "Introduction to (lithospheric) geodynamic modelling"
 - Our focus is on the **lithosphere**
 - Outermost layer of the Earth that is rigid over geological timescales
 - Thermal lithosphere: Portion of outer layers below ~1300°C
 - Crust and lithospheric mantle
 - No convecting mantle



Dissecting the course title

- This course is titled "Introduction to **geodynamic** modelling"
 - Our focus is on **geodynamics**
 - Plate tectonics and related phenomena
 - Physical processes/topics
 - Stress and strain
 - Heat transfer
 - Deformation: Faulting and folding, rheology



Dissecting the course title

- This course is titled "Introduction to geodynamic modelling"
 - Our focus is on **modelling**
 - Using computers to solve equations and simulate geodynamic processes
 - We will learn how to solve equations using numerical methods, and how to implement those numerical solutions in computer code
 - Few geodynamic processes are simple enough to be explored without the use of computers



The path forward

- Now we will briefly review the different physical processes and concepts related to geodynamics
- In the following lecture we'll take some of the equations we'll see in this lecture and discuss what is needed to solve them
- In the afternoon we will review basic computing concepts by way of examples using the Python programming language

Some of this will be review for you, but it never hurts to revisit these fundamental topics before moving on to more challenging topics



Plate Tectonics and related phenomena

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Lithospheric geodynamic processes

The Wilson cycle







Stüwe, 2007

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The focus for this lecture will be on the lithosphere and the dynamic processes involved in its deformation and evolution

 Many of these processes can be directly linked to Plate Tectonics and the Wilson cycle

Rifting of the lithosphere

Model 1E



(c) $t = 21 \text{ Ma}, \Delta x = 210 \text{ km}$







Stüwe, 2007

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Oceanic subduction



Currie et al., 2015

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Alpine-type Model S Tectonics and Velocity





T contours every 100°C, starting at 100°C



Alpine-type Model S Tectonics and Velocity





T contours every 100°C, starting at 100°C

Toward three dimensions

Rifting



Allken et al., 2012

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Continental collision



Braun and Yamato, 2010



Fold-and-thrust belt growth and erosion



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Fold-and-thrust belt growth and erosion



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What is a model?

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- "A **model** it tool used to <u>describe the world around us</u> in a *simplified way* so that we can *understand it better*"
 - Stüwe, 2007



What is a model?



 "A model it tool used to <u>describe the world around us</u> in a simplified way so that we can understand it better"

<u>Stüwe, 2007</u>

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- **Tectonic diagrams** are a familiar form of model to help clarify the time evolution of a study area
 - Typically this kind of model is used to simplify the complex modern geology and restore it to a predeformation state
 - These models, though, have no basis in physics



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- 3D structural or geological models are closer to reality in that they are based on a combination of surface and subsurface geological and geophysical observations
- The primary goal of these models is data visualisation, again helping us understand complex geometries
- Models of this type typically do not simulate physical processes

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Integrated geophysical modelling



Integrated geophyiscal models use a combination of an input crustal structure and composition, and rock thermal properties to calculate various properties of the lithosphere (gravity anomalies, seismic velocities, surface heat flow, etc.)

• These models involve a 2D or 3D geometrical model and calculation of heat transfer in the lithosphere and upper mantle

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• Thermo-kinematic (or thermokinematic) models

simulate both mass transport and heat transfer using a predefined velocity field and input rock thermal/physical properties

 Models of this type can be compared to a number of observables, including surface heat flow and mineral cooling ages, and typically have a geometry based on surface geological observations and geophysical data such as reflection seismics





- Thermo-mechanical models simulate true lithospheric dynamics
 - Internal deformation in the model is determined based on physical forces acting on the model and material properties of rock in the model
 - Heat transfer will vary as a result of model deformation, but also affect the model material properties





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- Thermo-mechanical models truly simulate lithospheric dynamics
 - This type of model offers the greatest predictive power, but can be difficult to directly link to geological observations because the model evolution is not known *a priori*
 - This kind of model is the focus for the remainder of this presentation





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Analogue versus numerical models



Tapponnier et al., 1982

Analogue models are an alternative to thermomechanical models where materials analogous to Earth materials are used to simulate deformation of the Earth in physical models

- These models do not prescribe any material behavior, but rather allow the material to deform subject to imposed deformation at the boundaries
- Though these are a viable alternative to numerical models, it is difficult to simulate temperature-dependent materials and scaling of the model properties can be a problem



Physical model concepts: Earth as a continuum

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What does that even mean?



Velocities and strain rates in a lithospheric geodynamic model

- Most geodynamic models treat the Earth as a **continuum** such that there are no material gaps or voids at the macroscopic scale
 - Field variables such as pressure, velocity, or stress are thus fully continuous
- In this context the Earth is a fluid with a very high viscosity (typically 10¹⁸ - 10²³ Pa s)



Earth as a fluid? Even the lithosphere?

• Fluid: Any material that flows in response to an applied stress

• Differences between **solids** and **fluids**

Solids	Fluids
Strain from being stressed	Continuous deformation under applied forces
Stresses related to strains	Stresses related to rates of strain
Strain result of displacement gradients	Strain result of velocity gradients

• Rheological (or constitutive) law: An equation relating stress to strain rates in a fluid



• Fluid mechanics is the science of fluid motion



Fluid mechanics

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- Based on conservation of three basic physical property and their corresponding mathematical representations
 - **Conservation of mass** The continuity equation
 - **Conservation of momentum** The momentum equation
 - **Conservation of energy** The heat transfer equation



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• Conservation of mass, momentum and energy are combined with rheological laws to <u>describe fluid movement under an applied force</u>



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- Calculations in the continuum are performed by considering an infinitesimal volume of the material, the local volume
- The general form of **conservation of mass** for a local volume of a continuum in an Eulerian reference frame is

 \mathbf{A}

$$\frac{\partial \rho}{\partial t} + \rho \left(\nabla \cdot V \right) = 0$$
Change in local density Mass or volume flux (divergence of velocity)
where ρ is the local density, t is time and V is the local velocity

$$\frac{\partial \rho}{\partial t} = -\rho \left(\nabla \cdot \boldsymbol{V} \right) \quad \text{ Alternative form }$$



The continuity equation

- It is common in geodynamic numerical models, particularly in the crust or lithosphere, to assume the <u>material is</u> <u>incompressible</u>
- In this case, the **continuity equation** simplifies to

$$\nabla \cdot \boldsymbol{V} = 0$$

stating simply that there is no divergence in the velocity field of the continuum

In many numerical models, this condition is not strictly obeyed, allowing a very small amount of compressibility in the materials

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What drives a fluid to flow?



• At this point, we have established that geodynamicists often model the Earth as a continuous, highly viscous fluid. Since we're interested in the dynamics of this fluid, a reasonable question to ask is what forces might cause a fluid to flow?

Sir George Stokes

The momentum equation



Sir George Stokes

The basic relationship that thus determines the dynamics of material in the continuum is conservation of momentum, the balance of internal and external forces acting on the material

The conservation of momentum for a fluid subject to gravity is the Navier-Stokes equation

$$\nabla \cdot \eta (\nabla \boldsymbol{V} + \nabla \boldsymbol{V}^{\mathrm{T}}) - \nabla P - \rho g = \rho \dot{\boldsymbol{V}}$$

Fluid velocity Fluid pressure Body forces Acceleration where η is the fluid shear viscosity, P is pressure, g is the acceleration due to gravity, and \dot{V} is the material time derivative of the fluid velocity (acceleration)

The momentum equation



Sir George Stokes

 For highly viscous fluids with a very small Reynolds number <u>the acceleration term of the Navier-Stokes</u> <u>equation can be ignored</u> reducing to the equation of **Stokes flow** (and simplifying the solutions)

$$\nabla \cdot \eta (\nabla V + \nabla V^{\mathrm{T}}) - \nabla P = \rho g$$

Fluid velocity Fluid pressure Body forces

 It is trivial to demonstrate that the Reynolds number of most geodynamic flows is extremely low

$$\mathbf{Re} = \frac{\rho V I}{n}$$

Inertial forces Viscous forces

The Reynolds number



- The Reynolds number determines whether or not a fluid flow should be expected to be turbulent or laminar
 - The critical value of the Reynolds number is ~2000, above which flow is turbulent

- Using your best guess at the equation values, estimate the Reynolds number for convection of the upper mantle
 - Do we need to worry about turbulence?

The Reynolds number

 $\mathbf{Re} =$



Physical model concepts: Stress and strain



- Force: <u>A push or pull applied to a body</u>.
 Force = mass x acceleration (Newton's second law)
- **Units**: Newtons [N]; 1 N = 1 kg m s⁻²



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Body forces versus surface forces

- **Body force**: Forces that <u>act throughout the volume of a</u> <u>solid</u>. <u>Proportional to its volume or mass</u>.
 - Example: Slab pull (gravity)

- Surface force: Forces that <u>act on the surface area bounding</u> <u>an element or volume</u>. <u>Proportional to the area upon which</u> <u>the force acts</u>.
 - Example: Friction along a fault plane



- **Stress**: A force per unit area transmitted through a material by interatomic force fields
- **Surface stress**: A pair of equal and opposite forces acting on the area of a surface in a specific orientation

Surface stresses

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 - Units: Pascals [Pa]; $1 \text{ Pa} = 1 \text{ N m}^{-2}$
 - **Representation**: Pair of vectors with a specified surface area/orientation
 - **Example**: Hand pushing on table, table pushing back

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Surface stress Component surface stresses



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after Twiss and Moores, 2006

Stress in two dimensions

Surface forces in 2D



- In two dimensions, we consider forces acting on four faces of an infinitesimal cube of dimension $\delta x \times \delta y \times \delta z$
 - Here we assume no forces act or vary in the *z* direction

Fig. 2.13, Turcotte and Schubert, 2014

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Stress in two dimensions

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- Normal stresses: σ_{xx} , σ_{yy}
- Shear stresses: σ_{xy} , σ_{yx}
- At equilibrium we can state $\sigma_{xy} = \sigma_{yx}$

Stress in two dimensions

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- Here we assume no forces act or vary in the *z* direction
- Normal stresses: σ_{xx} , σ_{yy}
- Shear stresses: σ_{xy} , σ_{yx}
- At equilibrium we can state $\sigma_{xy} = \sigma_{yx}$

• Why?



Stress in three dimensions



- In three dimensions, we consider forces acting on all six faces of an infinitesimal cube of dimension $\delta x \times \delta y \times \delta z$
- Normal stresses: σ_{xx} , σ_{yy} , σ_{zz}
- Shear stresses: σ_{xy} , σ_{yx} , σ_{xz} , σ_{zx} , σ_{yz} , σ_{zy}
- At equilibrium we can state $\sigma_{xy} = \sigma_{yx}, \sigma_{xz} = \sigma_{zx},$ $\sigma_{yz} = \sigma_{zy}$

Fig. 2.15, Turcotte and Schubert, 2014





Fig. 2.15, Turcotte and Schubert, 2014



Physical model concepts: Heat transfer

Why does temperature matter?

Rosenberg et al., 2007







- Rock deformation strongly depends upon temperature
 - Rock strength drops 80-90% for even small amounts of partial melt (5-7%)
 - Whether rocks are brittle and fault, or ductile and fold is largely determined by temperature



Heat transfer processes in the lithosphere

• Conduction

• **Production**

Advection



Heat transfer processes in the lithosphere

• Conduction: The diffusive transfer of heat by <u>kinetic atomic</u> or molecular interactions within the material. Also known as thermal diffusion.

Production





Fourier's first law of heat conduction

• In ID, the mathematical translation of "Heat flux *q* is *directly* proportional to the thermal gradient in a material" is

$$q_z = -k\frac{dT}{dz}$$

- Here, *T* represents temperature and *z* represents spatial position, depth in the Earth for our example
- Thus, *dT/dz* is the change in temperature with depth, or the **thermal gradient**
- The proportionality constant k is known as the thermal conductivity



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Heat transfer processes in the lithosphere

• **Conduction**: The diffusive transfer of heat by <u>kinetic atomic</u> or molecular interactions within the material. Also known as thermal diffusion.

• **Production**: Not really a heat transfer process, but rather a source of heat. Sources in the lithosphere include radioactive decay, friction in deforming rock or chemical reactions such as phase transitions.

Advection



Radiogenic heat production

- Radiogenic heat production, *A* or *H*, is one of several heat sources and results from the <u>decay of radioactive isotopes in the</u> <u>Earth</u>, mainly ²³⁸U, ²³⁵U, ²³²Th and ⁴⁰K. *A* is often used for volumetric heat production and *H* for heat production by mass.
- These elements occur in the mantle, but are <u>concentrated in the</u> <u>crust</u>, where radiogenic heating can be significant
 - The surface heat flow in continental regions is ~65 mW m⁻² and ~37 mW m⁻² is from radiogenic heat production (57%)

Rock Type	U (ppm)	Concentration Th (ppm)	K (%)
Reference undepleted (fertile) mantle	0.031	0.124	0.031
"Depleted" peridotites	0.001	0.004	0.003
Tholeiitic basalt	0.07	0.19	0.088
Granite	4.7	20	4.2
Shale	3.7	12	2.7
Average continental crust	1.42	5.6	1.43
Chondritic meteorites	0.008	0.029	0.056



Heat transfer processes in the lithosphere

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• Advection: The transfer of heat by <u>physical movement</u> of molecules or atoms within a material. A type of convection, mostly applied to heat transfer in solid materials.



Mathematical description of advection



Fig. 3.13, Stüwe, 2007

Advection in the vertical direction at velocity v_z at steady state can be represented mathematically as

$$v_z \frac{dT}{dz} = 0$$

- Note that this equation simply describes the vertical translation of temperatures, and that in order for any change in temperature to occur, advection must be combined with other heat transfer processes such as conduction
- In general, we can describe heat advection as

 $\boldsymbol{V}\cdot\nabla T=0$



The heat conservation equation

- We now combine our three heat transfer components (conduction, production, advection) into the heat conservation equation, which describes heat transfer subject to each of these processes
- In one dimension (vertical), this equation is



 Alternatively, we can state the same equation in substituting in Fourier's first law for the heat flux q

$$\rho c_P \left(\frac{\partial T}{\partial t} + v_z \frac{\partial T}{\partial z} \right) = \frac{\partial}{\partial z} \left(k \frac{\partial T}{\partial z} \right) + A$$



The heat conservation equation

- We now combine our three heat transfer components (conduction, production, advection) into the heat conservation equation, which describes heat transfer subject to each of these processes
- In general, we can state

$$\rho c_P \left(\frac{\partial T}{\partial t} + \boldsymbol{V} \cdot \nabla T \right) = \nabla \cdot k \nabla T + A$$

$$\boldsymbol{f} \quad \boldsymbol{f} \quad \boldsymbol$$



Physical model concepts: Rheological laws



Rheology of the lithosphere

- The term **rheology** refers to the flow characteristics of materials
 - For most geoscientists this term describes the <u>deformation</u> <u>behavior of materials</u> regardless of whether deformation occurs by flow, fracture, or other mechanisms

- Rock deformation mainly occurs by three deformation mechanisms:
 - Elasticity
 - Plasticity
 - Viscous flow



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- Rock deformation mainly occurs by three deformation mechanisms:
 - Elasticity Can ignore this, not relevant for long time scales
 - Plasticity
 - Viscous flow



Perfectly plastic behavior

Twiss and Moores, 2007

- **Constant stress** required for deformation
 - No deformation prior to exceeding yield stress
 - Infinite deformation if applied stress equals (or exceeds) yield stress
 - $\sigma < \sigma_{\rm y}$ no deformation
 - $\sigma = \sigma_y$ failure; infinite deformation
- Nonrecoverable






Perfectly plastic behavior

- **Constant stress** required for deformation
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Normal stress

$$\sigma_{\rm n} = \frac{mg\cos\theta}{A}$$
$$\sigma_{\rm s} = \frac{mg\sin\theta}{A}$$

Shear stress

- Fault slip accounts for a large portion of deformation of the upper crust
- Friction must be overcome for slip to occur
 - After exceeding the frictional resistance, slip will occur on the fault or shear zone
 - Known as **frictional plasticity**
 - The basic relationship for static friction is $au_{f_{
 m s}} = f_{
 m s}\sigma_{
 m n}$ (Amonton's law)

where f_s is the **coefficient of static** friction, and τf_s is the static frictional stress required for slip

(Linear) Viscous deformation

• In simple shear,

 $au_{
m s}=\eta\dot{\gamma}$ η Dynamic viscosity

Shear stress proportional to shear strain rate

• In general,

 $\boldsymbol{\tau} = 2\eta \dot{\boldsymbol{\varepsilon}}$

deviatoric stress is proportional to **strain rate**

- For linear viscous (Newtonian) materials, η is constant
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В.

(Linear) Viscous deformation

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- For linear viscous (Newtonian) materials, η is constant
- Nonrecoverable



Nonlinear viscous deformation

- Most rocks <u>do not</u> behave as Newtonian viscous materials
- Why not?
- Two main reasons:
 - Temperature dependence

 $\eta = A_0 e^{Q/RT_{\rm K}}$

 A_0 is the pre-exponent constant, Q is the activation energy, R is the universal gas constant and T_K is temperature in Kelvins



Stüwe, 2007

Nonlinear viscous deformation

- Most rocks <u>do not</u> behave as Newtonian viscous materials
- Why not?
- Two main reasons:
 - Nonlinearity

 $\tau_{s}^{n} = A_{eff} \dot{\gamma}$ *n* is the power law exponent and A_{eff} is a material constant in Paⁿ s

 Many rocks <u>deform 8 times as fast</u> <u>when stress is doubled</u>





Lithospheric strength envelopes

 There are many ways in which lithospheric strength can be modelled, here are a few

• Jelly sandwich

- A Brace-Goetze
- B Wet LC

• Crème brûlée

- C Wet UM
- D Wet LC, UM



- The aim of this course is to help you understand geodynamic models (mainly in the lithosphere)
 - The models are (thermo-)mechanical, where the internal and external forces acting on the extremely viscous fluid in the model determine how the model will deform
 - The physics and general concepts of the equations are fairly simple, but as you will see, the numerical solution of the equations and the output can be complex



- Deformation of the Earth in numerical geodynamic models is based on three simple conservation equations
 - **Conservation of mass** The continuity equation
 - **Conservation of momentum** The momentum equation
 - **Conservation of energy** The heat transfer equation

 Conservation of mass, momentum and energy are combined with rheological laws to <u>describe fluid movement under an</u> <u>applied force</u>



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78





80



 $\sigma_{n} \text{ or } \sigma_{s}$ Slope = E or 2G $\varepsilon_{n} \text{ or } \varepsilon_{s}$

 $\pmb{\sigma}\propto \pmb{arepsilon}$

- **Stress** is proportional to **strain**
- For I-D normal stress
 - $\sigma_{xx} = E \varepsilon_{xx}$ E: Young's modulus (ID) G: Shear modulus (ID)
- If stress $\rightarrow 0$, strain $\rightarrow 0$ (recoverable)

А.

 $F = k_1 \Delta x$



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